

COMPONENTS OF A VECTOR.

A unit vector is a vector of magnitude 1.

A unit vector is denoted by \hat{a} .

\hat{a} is the unit vector with the same direction as \underline{a}

$$\hat{a} = \frac{\underline{a}}{|\underline{a}|}$$

* Cartesian Form

The unit vector in the +ve direction of the x-axis is \hat{i}

The unit vector in the +ve direction of the y-axis is \hat{j}

The unit vector in the +ve direction of the z-axis is \hat{k} .

- Two Dimensions

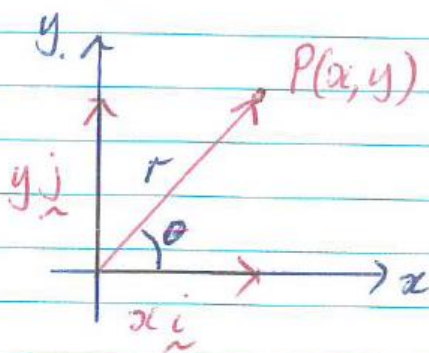
For the point $P(x, y)$.

$$\vec{OP} = x\hat{i} + y\hat{j}$$

$$|\vec{OP}| = r = \sqrt{x^2 + y^2}$$

Direction

$$\tan \theta = \frac{y}{x}$$



- Three Dimensions

For the Point $P(x, y, z)$.

$$\vec{OP} = x\vec{i} + y\vec{j} + z\vec{k}$$

$$|\vec{OP}| = r = \sqrt{x^2 + y^2 + z^2}$$

Direction made with an axis

$$\text{x-axis } \cos \alpha = \frac{x}{|\vec{OP}|}$$

$$\text{y-axis } \cos \beta = \frac{y}{|\vec{OP}|}$$

$$\text{z-axis } \cos \gamma = \frac{z}{|\vec{OP}|}$$

